## Chapter 9: Polynomials and Factoring Study Guide

## 9.1: Add and subtract polynomials:

- Be able to identify an expression as a polynomial or not. If it is, be able to classify it by the number of terms, find the degree and write it so it is in descending order.

| Expression | Pol <br> y <br> om <br> ial <br> ? | Type | Degree | Descending Order |
| :---: | :---: | :---: | :---: | :---: |
| $-1 / 2$ |  |  |  |  |
| $x^{3} y^{5} z$ |  |  |  |  |
| $3 x+\frac{1}{x}$ |  |  |  |  |
| $7 b c^{3}+4 b^{4} c$ |  |  |  |  |
| $5 a b^{3} c^{5}-4 a^{2} b c^{2}+3 a^{3} b^{3} c$ |  |  |  |  |
| $5 z+2 z^{3}-z^{2}+3 z^{4}$ |  |  |  |  |
| $-8 r s^{2}+3 r^{2} s-4 r^{2} s^{2}+9 r-3 s$ |  |  |  |  |

- Be able to add and subtract polynomials:

Ex: $\left(9 x+6 x^{3}-8 x^{2}\right)+\left(-5 x^{3}+6 x\right) \quad$ Ex: $\left(2 s^{3}+8\right)-\left(-3 s^{3}+7 s-5\right)$

## 9.2 - 9.3: Multiply Polynomials/Special Products Formulas:

- Be able to distribute, FOIL and multiply polynomials
Ex: $(-3 d+10)(2 d-1)$
Ex: $(2 s+5)\left(s^{2}+3 s-1\right)$

Ex: $(m+7)(m-3)-(m-4)(m+5)$

- Be able to apply special products formulas
Ex: $(3 m-7 n)^{2}$
Ex: $(3 x+8 y)^{2}$
Ex: $(2 a-5 b)(2 a+5 b)$

Ex: You are designing a rectangular flower bed that you will border using brick pavers. The width of the border around the bed will be the same on every side, as shown.
a. Write a polynomial that represents the total area of the flower bed and the border.
b. Find the total area of the flower bed and border when the width of the border is 1.5 feet.


## 9.4: Factor Using the GCF:

- Be bale to identify the GCF of a quadratic expression and factor using this method.
Ex: $2 x^{2}-4 x$
Ex: $-4 y+16 y^{2}$
Ex: $3 x y+8 x y^{2}$
- Be able to solve a quadratic equation in factored form.
Ex: $(3 x-1)(x+2)=0$
Ex: $x(2 x-5)=0$
Ex: $x(3 x-7)(4 x-1)=0$
- Be able to solve a quadratic equation by factoring using the GCF first!
Ex: $7 x^{2}+21 x=0$
Ex: $8 x^{2}-16 x=0$
Ex: $2 x^{2}=-7 x$
- Be able to use the vertical motion model to solve problems involving a problem's height and time. $\left(h=-16 t^{2}+v t+s\right)$

Ex: An object is launched from the ground with an initial vertical velocity of 32 feet per second. How long before the object reaches the ground?

## 9.5: Factor Quadratics in the Form $y=x^{2}+b x+c$ :

- Be able to factor trinomials in the form $x^{2}+b x+\mathrm{c}$ by factoring into two binomials in the form:

$$
(x+p)(x+q)
$$

Ex: $x^{2}-7 x+12$
Ex. $x^{2}-2 x-24$
Ex: $-x^{2}-9 x-18$

- Be able to solve quadratic equations by factoring first.
Ex: $x^{2}-7 x+12=0$
Ex: $x^{2}-17 x+60=0$
Ex: $x^{2}+8 x=-12$
- Be able to use the vertical motion model to solve problems involving a problem's height and time. $\left(h=-16 t^{2}+v t+s\right)$

Ex: An object is launched from a height of 48 feet with an initial vertical velocity of 32 feet per second. How long before the object reaches the ground?

## 9.6: Factor Quadratics in the Form $y=a x^{2}+b x+c$ :

- Be able to factor quadratics in the form $y=a x^{2}+b x+c$ into two binomials either using the $a x^{2}+m x+n x+c$ method or number combinations method.
Ex: $3 x^{2}+x-2$
Ex: $5 x^{2}-6 x+1$
Ex: $3 x^{2}+13 x+4$
- Be able to solve quadratics in the form $y=a x^{2}+b x+c$ by factoring first.
Ex: $3 x^{2}+x-2=0$
Ex: $2 x^{2}-3 x-35=0$
Ex: $4 x^{2}+11 x=3$


## 9.7: Factor Special Products:

- Be able to factor difference of two squares
Ex: $x^{2}-25$
Ex: $4 x^{2}-169$
Ex: $2 x^{2}-50$
- Be able to factor perfect square trinomials
Ex: $4 x^{2}+20 x+25$
Ex: $3 x^{2}-8 x+48$


## 9.8: Factor Polynomials Completely:

- Be able to factor out a common binomial

Ex: $x(x-8)+(x-8)$
Ex: $5 y(y+3)-2(y+3)$
Ex: $6 z(z-4)+5(4-z)$

- Be able to factor by grouping

Ex: $5 n^{3}-4 n^{2}+25 n-20$
Ex: $y^{2}+5 x+5 x y+y$

- Be able to factor polynomials completely

Ex: $7 a^{3} b^{3}-63 a b^{3}$
Ex: $-4 s^{3} t^{3}+24 s^{2} t^{2}-36 s t$

Ex: $6 g^{3}-24 g^{2}+24 g$
Ex: $3 n^{5}-48 n^{3}$

